#### **Two- and Multi-Party Protocols** JASS 2005

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#### Why cryptographic protocols?

# Why cryptographic protocols?

- cryptography is concerned with secure communication
- various other tasks
- enable to solve many real-world problems electronically
- theoretical any given functionality can be performed with protocols

∇ Two- and Multi-Party Protocols – p.2/43



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But what's that! All printers in the department seem to malfunction. So Joe needs a way to electronically timestamp his work.















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- no privacy (transmission, database)
- no efficiency (huge database)
- errors may occure (transmission, database)
- third party may not be honest







We use one-way hashfunctions and digital signatures to enhance the protocol.



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- privacy (only hash is revealed)
- efficiency (no database is needed)
- no errors (examine signed hash immediately)
- remaining Problem: Joe and Anja might work together















This protocols makes it very hard for Joe to cheat.
# **Timestamping - Final Try (II)**

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- for selection: random-number-generator with hash of document as input
- choose k sufficiently high
- only a subset of k persons should suffice for a valid timestamp

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## **Mental Poker - Requirements**

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- Joe generates 52 messages  $M_1, M_2, \ldots, M_{52}$
- unique random string

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- Joe generates 52 messages  $M_1, M_2, \ldots, M_{52}$
- unique random string
- $E_J(M_i) := M_i$  encrypted with Joes public-key'
- $D_S(X) := X$  decrypted with Steves private-key'
- cryptographic algorithm commutative, i.e.  $D_S(E_L(E_S(X))) = E_L(X)$



















#### **Mental Poker - Discussion**

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- additional cards
- everyone reveals his hand and keys after the game
- desired: only winner reveals his hand, but this is not secure
- implementation is not effective

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'Maybe next week I should try this with Lee from Tokyo?'













#### **Bit Commitment - Discussion**

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- random-bit string is important
- impossible to cheat
- several other protocols for this task
- e.g. involving one-way functions or pseudo-random-sequence generators

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Steve:'Ok, I will show you how.'









Steve explains following protocol, which uses a one-way function f. Steve chooses a random number r



'Your guess is right so its heads'



# **Coin Flipping - Discussion**

∇ Two- and Multi-Party Protocols – p.18/43

# **Coin Flipping - Discussion**

- security rests in one-way function
- least significant bit of f(x) and x must be uncorrelated
- use some other bit
- several other protocols exist

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Hi Joe!

I heard you wrote a paper on  $P \neq NP$ . I'd love to write something about it in the 'Computer Science Weekly'.

I'd pay you if you would give me a copy before you publish it.

Call me a.s.a.p.

Bye, Anja

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'I'll give you half the pages for half the price. You will get a good impression of my work and I get the money it is worth.

Anja:'Ok, but I want to choose the pages, so you don't send me the boring ones.'

# **Oblivious Transfer - Requirements**

⊽ Two- and Multi-Party Protocols – p.20/43

# **Oblivious Transfer - Requirements**

- Anja will receive only half of the pages
- Joe will not know which pages Anja receives
- Here: Joe sends Anja one of two messages  $M_1, M_2$
- Joe generates two public-key/private-key pairs  $K_1, K_2$
- Anja chooses a key K<sub>A</sub> in a symmetric algorithm (e.g. DES)









#### **Oblivious Transfer - Discussion**

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- one message is gibberish
- other is plain
- Joe may encrypt two identical messages
- reveal Joes private-key later
- protocol is strange but useful

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Reto the bank clerk first explains to Joe, what a blind signature is.

# **Blind Signatures - Requirements**

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# **Blind Signatures - Requirements**

- Reto shall sign a document without knowing the content
- in real-life: envelope and carbon paper
- signature function S commutes with an encryption Ei.e. D(S(E(m)) = S(m)
- RSA and one-time pads









#### **Blind Signature - Discussion**

∇ Two- and Multi-Party Protocols – p.26/43

# **Blind Signature - Discussion**

- when Joe decrypts he gets the signed message
- Reto can not know which document he signed
- Reto can even get the signed document
- Reto signs many documents
- 'Reto owes Joe \$ 1.000.000'

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Joe immediately senses a new possibility of making money. He urges Reto to go on quickly, but Reto refuses. He wants Joe to understand the problems involved with digital money. 'I will first tell you what is important about digital money.'

#### **Digital Cash - Requirements**

∇ Two- and Multi-Party Protocols – p.28/43

# **Digital Cash - Requirements**

- forgery has to be prevented or detected
- duplication has to be prevented or detected
- customers' anonymity has to be preserved
- no audit trails
- efficiency

#### **Blind Signature enhanced**

We want to prevent Joe from cheating.

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- present 100 documents to Reto
- Reto opens 99 documents at random
- all 99 documents should have the same content

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- Payment: verify signature
- Deposit: verify signature and then credit \$ 1000

#### **DC Protocol # 1 - Discussion**

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#### **DC Protocol # 1 - Discussion**

- anonymity
- no cheating
- double spending problem'

To solve the double spending problem we alter the protocol as follows.

random uniqueness string for each money order

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- string should be long enough
- Deposit: verify uniqueness string has not been used already

Protocol # 2 does prevent cheating but does not identify the cheater. So we will alter the protocol some more.

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  - uniqueness and identity string in the database then the merchant cheated

#### **Money Order**

⊽ Two- and Multi-Party Protocols – p.34/43

#### **Money Order**

before payment

Amount uniqeness string

Signature

#### **Money Order**



#### **DCP # 4 Money Order Creation**

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- $\bullet$  *n* pairs of identity bit strings generated as follows
- an identity string stating Joes name, address, etc.
- split this into two pieces using a 'secret splitting protocol'
- commit to each piece (bit-commitment)
- any pair reveals Joes identity when opened (e.g.  $I_{23_L}$  and  $I_{23_R}$  but not  $I_{23_L}$  and  $I_{42_R}$ )

# **Money Order - After Withdrawal**

⊽ Two- and Multi-Party Protocols – p.36/43

# **Money Order - After Withdrawal**

after withdrawal



# **DCP # 4 Withdrawal and Payment**

⊽ Two- and Multi-Party Protocols – p.37/43

# **DCP # 4 Withdrawal and Payment**

- Withdrawal: Reto verifies that all 99 messages are well formed
  - amount
  - uniqueness string
  - all identity strings

# DCP # 4 Withdrawal and Payment

- Withdrawal: Reto verifies that all 99 messages are well formed
  - amount
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  - all identity strings
- Payment: merchant will give Joe a random n-bit selector string b
- Joe will open either the left or right half, depending on b
- the random identity string is not used anymore

#### **Money Order - identity strings**
# **Money Order - identity strings**

before payment



# **Money Order - identity strings**



 $I_{n_L} = I_{n_R}$ 

Signature

Amount uniqeness string  $I_{1_L} = I_{1_R}$  $I_{2L}$   $I_{2R}$  $I_{3L} = I_{3R}$  $I_{n_L} = I_{n_R}$ Signature

#### DCP # 4 - Deposit

⊽ Two- and Multi-Party Protocols – p.39/43

# DCP # 4 - Deposit

- Deposit: Reto will check signature and uniqueness string
  - if uniqueness string is not used yet, record it and all the identity information
  - if the money is double spent, compare identity information
  - if they are identically the merchant has cheated
  - if not identity information is revealed

#### **Digital Cash - Summary**

Two- and Multi-Party Protocols – p.40/43

# **Digital Cash - Summary**

- forgery is prevented by eBSP
- duplication is detected with uniqueness string
- customers' anonymity is preserved, as long as he does not cheat
- no audit trails exist, as long as the customer does not cheat
- efficiency

Since Joe has now fully understand digital cash and the protocol, he will probably withdraw his first \$ 1000 bill tomorrow.

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If Joes proof of  $P \neq NP$  really holds you may read in the next volume of 'Computer Science Weekly'

#### The End

That's it. (Just kidding)

#### The End

Thank you for your attention.